

Introduction to Computing

Basics of Python Programming – III

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September, 2024

1 Functions

2 Importing Modules and Functions

3 Mathematical Functions

- Mathematical Functions for Real Numbers
- Mathematical Functions for Complex Numbers

4 Statistical Functions

Functions

```
def <function-name>(<argument 1>, ..., <argument n>):  
    Statement 1  
    Statement 2  
    Statement 3  
    return <expression>
```

Functions

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def <function-name>(<argument 1>, ..., <argument n>):  
    Statement 1  
    Statement 2  
    Statement 3  
    return <expression>
```

Note: You may either return a values obtained from an <expression> or return nothing based on your requirement.

Functions – Understanding the internals

```
def function(a, b, c):  
    print('Inside 1:', hex(id(a)), hex(id(b)), hex(id(c)))  
    b += 10  
    print('Inside 2:', hex(id(a)), hex(id(b)), hex(id(c)))  
x, y, z = 10, 10, 20  
print('Outside:', hex(id(x)), hex(id(y)), hex(id(z)))  
function(x, y, z)
```

Functions – Understanding the internals

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def function(a, b, c):  
    print('Inside 1:', hex(id(a)), hex(id(b)), hex(id(c)))  
    b += 10  
    print('Inside 2:', hex(id(a)), hex(id(b)), hex(id(c)))  
x, y, z = 10, 10, 20  
print('Outside:', hex(id(x)), hex(id(y)), hex(id(z)))  
function(x, y, z)
```

Output:

```
Outside: 0x7fc4436a0210 0x7fc4436a0210 0x7fc4436a0350  
Inside 1: 0x7fc4436a0210 0x7fc4436a0210 0x7fc4436a0350  
Inside 2: 0x7fc4436a0210 0x7fc4436a0350 0x7fc4436a0350
```

Comparing the lengths of two positive integers

```
def compare(m, n):
    while m and n:
        m //= 10
        n //= 10
    return m-n
x, y = input('Enter two numbers: ').split()
f = compare(int(x), int(y))
if f > 0:
    print(x, 'has larger number of digits')
elif f < 0:
    print(y, 'has larger number of digits')
else:
    print('Both have same number of digits')
```

Finding prefixes of a string

```
def prefix(str):
    start, end = 0, 0
    while start < len(str):
        if str[end] == str[end-start]:
            print(str[start:end + 1], end= " ")
            end += 1
            if end == len(str):
                start += 1
                end = start
        else:
            start += 1
            end = start # Index of substring
```

Input: prefix('Python')

Lambda functions

Python provides an anonymous function `lambda` that can take any number of arguments, but can only have one expression.

```
x = lambda a: a + 10
print(x(5))
```

Here, the output will be 15. **Note:** Lambda functions execute comparatively faster (in general) because they are inline functions.

Lambda functions

```
a, b = 3, 5
maximum = lambda a, b: a if a > b else b
print(f'{maximum(a,b)} is the maximum among', a, 'and', b)
```

Lambda functions

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```

Output:

```
5 is the maximum among 3 and 5
```

Lambda functions

```
l = lambda n: n
q = lambda n: n ** 2
c = lambda n: n ** 3
x = 2
y = c(x) + 3*q(x) + 2*l(x) + 1 # y = x^3 + 3x^2 + 2x + 1
print(y)
```

Lambda functions

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q = lambda n: n ** 2
c = lambda n: n ** 3
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print(y)
```

Output:

25

Late binding closures

Python's closures are **late binding**. Hence, the values of variables used in closures are looked up when the inner function is called.

```
def increase():  
    return [lambda x : i + x for i in range(5)]  
for add in increase():  
    print(add(10))
```

Here, whenever any of the returned functions are called, the value of i is looked up in the surrounding scope at call time. By then, the loop has completed and i is left with its final value of 4. So, it will print $\{14, 14, 14, 14, 14\}$ instead of $\{10, 11, 12, 13, 14\}$.

Importing modules and functions

Importing a module:

```
import <module_name>
```

OR

```
import <module_name> as <custom_name>
```

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Using a function:

```
import <module_name>  
<module_name>.<function_name>()
```

OR

```
import <module_name> as <custom_name>  
<custom_name>.<function_name>()
```

OR

```
from <module_name> import <function_name>  
<function_name>()
```

Using built-in methods

There are some functions in Python that does not require to import a module because they work on specific data structures.

- Built-in methods for strings (e.g., `capitalize()`, `strip()`, `zfill()`, etc.)
- Built-in methods for lists/arrays (e.g., `sort()`, `reverse()`, `clear()`, etc.)
- Built-in methods for dictionaries (e.g., `keys()`, `values()`, `update()`, etc.)
- Built-in methods for tuples (e.g., `count()`)

Note: The `sort()` method in Python implements the hybrid algorithm *Timsort*, derived from merge sort and insertion sort.

Mathematical functions for real numbers

Using the `math` module:

```
import math
math.<function_name>()
```

Mathematical functions for real numbers

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```

ceil(x)	– Ceiling of x
comb(n, r)	– Number of ways to choose r from n (${}^n C_r$)
copysign(x, y)	– Float with magnitude of x but sign of y
fabs(x)	– Absolute value of x
factorial(x)	– Factorial of x
floor(x)	– Floor of x

Table: Functions in math module

Mathematical functions for real numbers

Library code of the factorial() function:

```
static PyObject * math_factorial(PyObject *module, PyObject *arg){
    ...
    /* use lookup table if x is small */
    if (x < (long)Py_ARRAY_LENGTH(SmallFactorials))
        return PyLong_FromUnsignedLong(SmallFactorials[x]);
    /* else express in the form odd_part * 2**two_valuation,
    and compute as odd_part << two_valuation. */
    odd_part = factorial_odd_part(x);
    if (odd_part == NULL)
        return NULL;
    two_valuation = x - count_set_bits(x);
    result = _PyLong_Lshift(odd_part, two_valuation);
    Py_DECREF(odd_part);
    return result;
}
```

Source: github.com/python/cpython/blob/main/Modules/mathmodule.c

Mathematical functions for real numbers

<code>fmod(x, y)</code>	– $x \% y$ (preferable for integers)
<code>frexp(x)</code>	– Mantissa and exponent of x as a pair (m, e)
<code>fsum(iterable)</code>	– Accurate floating point sum of values in iterable
<code>gcd(x, y)</code>	– GCD of the integers x and y
<code>isclose(x, y, *, rel_tol=1e-09, abs_tol=0.0)</code>	– Whether x is close to y w.r.t max/min allowed tolerance
<code>isfinite(x)</code>	– Whether x is finite (or ∞ /NaN)
<code>isinf(x)</code>	– Whether x is infinite
<code>isnan(x)</code>	– Whether x is NaN (“not a number”)
<code>isqrt(x)</code>	– Integer square root of x
<code>ldexp(x, i)</code>	– $x * 2^i$

Table: Functions in `math` module

Mathematical functions for real numbers

```
import math
print(sum([.1, .1, .1, .1, .1, .1, .1, .1]))
print(math.fsum([.1, .1, .1, .1, .1, .1, .1, .1]))
ls = [1/7, 1/7, 1/7, 1/7, 1/7, 1/7, 1/7]
print(sum(ls))
print(math.fsum(ls))
```

Output:

```
0.7999999999999999
0.8
0.9999999999999998
1.0
```

Mathematical functions for real numbers

<code>modf(x)</code>	– Fractional and integer parts of x
<code>perm(n, r=None)</code>	– Number of ways to choose k from n without repetition (${}^n P_r$)
<code>prod(iterable, *, start=1)</code>	– Product of values in iterable
<code>remainder(x, y)</code>	– Remainder of x when divided by y
<code>trunc(x)</code>	– Value of x truncated to an integral
<code>exp(x)</code>	– e^x
<code>expm1(x)</code>	– $e^x - 1$ (provides a better precision)
<code>log(x[, base])</code>	– Natural logarithm of x (base e)
<code>log1p(x)</code>	– Natural logarithm of $1+x$ (base e)
<code>log2(x)</code>	– Base-2 logarithm of x
<code>log10(x)</code>	– Base-10 logarithm of x
<code>pow(x, y)</code>	– x^y

Table: Functions in `math` module

Mathematical functions for real numbers

```
import math
print(math.exp(0.8) - 1)
print(math.expm1(0.8))
print(math.log(math.exp(0.8)))
print(math.log(math.expm1(0.8)+1))
```

Output:

```
1.2255409284924679
1.2255409284924677
0.8000000000000002
0.7999999999999999
```

Mathematical functions for real numbers

<code>sqrt(x)</code>	– Square root of x
<code>acos(x)</code>	– Arc cosine of x (result in radians)
<code>asin(x)</code>	– Arc sine of x (result in radians)
<code>atan(x)</code>	– Arc tangent of x (result in radians)
<code>atan2(x, y)</code>	– Arc tangent of x/y (in radians)
<code>cos(x)</code>	– Cosine of x
<code>dist(iterable1, iterable1)</code>	– Euclidean distance between iterable 1 and iterable2
<code>hypot(*coordinates)</code>	– Euclidean norm $\sqrt{x*x + y*y}$ for the point (x, y) , $\sqrt{\text{sum}(x**2 \text{ for } x \text{ in coordinates})}$
<code>sin(x)</code>	– Sine of x
<code>tan(x)</code>	– Tangent of x

Table: Functions in `math` module

Mathematical functions for real numbers

- degrees(x) – Convert angle x from radians to degrees
- radians(x) – Convert angle x from degrees to radians.
- acosh(x) – Inverse hyperbolic cosine of x
- asinh(x) – Inverse hyperbolic sine of x
- atanh(x) – Inverse hyperbolic tangent of x
- cosh(x) – Hyperbolic cosine of x
- sinh(x) – Hyperbolic sine of x
- tanh(x) – Hyperbolic tangent of x
- erf(x) – Error function at x
- erfc(x) – Complementary error function at x
- gamma(x) – Gamma function at x
- lgamma(x) – Natural logarithm of absolute value of Gamma function at x

Table: Functions in `math` module

Mathematical functions for real numbers

- pi – $\pi = 3.14\dots$, to available precision
- e – $e = 2.71\dots$, to available precision
- tau – $\tau = 6.28\dots$, to available precision
- inf – Floating-point positive infinity
- nan – Floating-point NaN

Table: Functions in `math` module

Mathematical functions for complex numbers

Using the `cmath` module:

```
import cmath  
cmath.<function_name>()
```

OR

```
from cmath import <function_name>  
<function_name>()
```

Mathematical functions for complex numbers

Using the `cmath` module:

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import cmath  
cmath.<function_name>()
```

OR

```
from cmath import <function_name>  
<function_name>()
```

<code>phase(x)</code>	– Phase of x (in float)
<code>polar(x)</code>	– Representation of x in polar coordinates as (r, ϕ)
<code>rect(r, phi)</code>	– Complex number x with polar coordinates r and ϕ
<code>exp(x)</code>	– e^x
<code>log(x[, base])</code>	– Natural logarithm of x (base e)
<code>log10(x)</code>	– Base-10 logarithm of x

Table: Functions in `cmath` module

Mathematical functions for complex numbers

<code>sqrt(x)</code>	– Square root of x
<code>acos(x)</code>	– Arc cosine of x
<code>asin(x)</code>	– Arc sine of x
<code>atan(x)</code>	– Arc tangent of x
<code>cos(x)</code>	– Cosine of x
<code>sin(x)</code>	– Sine of x
<code>tan(x)</code>	– Tangent of x
<code>acosh(x)</code>	– Inverse hyperbolic cosine of x
<code>asinh(x)</code>	– Inverse hyperbolic sine of x
<code>atanh(x)</code>	– Inverse hyperbolic tangent of x
<code>cosh(x)</code>	– Hyperbolic cosine of x
<code>sinh(x)</code>	– Hyperbolic sine of x
<code>tanh(x)</code>	– Hyperbolic tangent of x

Table: Functions in `cmath` module

Mathematical functions for complex numbers

<code>isclose(x, y, *, rel_tol=1e-09, abs_tol=0.0)</code>	– Whether x is close to y w.r.t max/min allowed tolerance
<code>isfinite(x)</code>	– Whether x is finite (or ∞ /NaN)
<code>isinf(x)</code>	– Whether x is infinite
<code>isnan(x)</code>	– Whether x is NaN
<code>pi</code>	– $\pi = 3.14\dots$, to available precision
<code>e</code>	– $e = 2.71\dots$, to available precision
<code>tau</code>	– $\tau = 6.28\dots$, to available precision
<code>inf</code>	– Floating-point positive infinity
<code>infj</code>	– Complex number with zero real and positive infinity imaginary parts
<code>nan</code>	– Floating-point NaN
<code>nanj</code>	– Complex number with zero real part and NaN imaginary part

Table: Functions in `cmath` module

Statistical functions

Using the statistics module:

```
import statistics
statistics.<function_name>()
```

Statistical functions

Using the statistics module:

```
import statistics
statistics.<function_name>()
```

mean(X) – Arithmetic mean of the data in X

fmean(X) – Arithmetic mean of the data (converted to float) in X

geometric_mean(X) – Geometric mean of the data (converted to float) in X

harmonic_mean(X) – Harmonic mean of the data in X

Table: Functions in statistics module

Statistical functions

<code>median(X)</code>	– Median of the data in X
<code>median_low(X)</code>	– Low median of the data in X
<code>median_high(X)</code>	– High median of the data in X
<code>median_grouped(X, interval)</code>	– Median of the grouped data in X
<code>mode(X)</code>	– Most frequent data item in X
<code>multimode(X)</code>	– Most frequent data items in the order they appear in X

Table: Functions in statistics module

Statistical functions

- `pstdev(X, mu=None)` – Population standard deviation of the data in X
- `pvariance(X, mu=None)` – Population variance of the data in X
- `stdev(X, xbar=None)` – Sample standard deviation of the data in X
- `variance(X, xbar=None)` – Sample variance of the data in X
- `quantiles(X, *, n, method)` – Divide data in X into n continuous intervals with equal probability

Table: Functions in statistics module

Homework

- Write a program that takes a string as input and pass it on to a function to print all its suffixes.
- Write a lambda function to return the maximum of three integers.
- Write a lambda function to compute the factorial of a number given as user input.
- The Maclaurin series of the exponential function e^x is given by

$$\sum_{n=0}^{\infty} \frac{x^n}{n!} = \frac{x^0}{0!} + \frac{x^1}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \frac{x^5}{5!} + \dots$$

Write a program to find out the value of e^x up to a number of terms given as user input.